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Dept :- Mechanical

Subject :- Design of Transmission Systems.

Year :- III / "A&B"

Sem :- VI

## UNIVERSITY PATTERN


11. (a) Flat belt  $\left\{ \begin{array}{l} \text{General procedure} \\ \text{From equation [Find: } T_1 \text{ \& } T_2] \end{array} \right.$
- V-belt  $\left\{ \begin{array}{l} \text{General Procedure [Types].} \\ \text{From equ}^n \end{array} \right.$

(OR)

(b) Chain drives.


(OR)

Pope [2% only chance]


12. (a) Spur Gear  $\left\{ \begin{array}{l} \text{Static [General]} \\ \text{Dynamic [Lewis method]} \end{array} \right.$
- 

(OR)

- (b) Helical Gear  $\left\{ \begin{array}{l} \text{Static [General]} \\ \text{Dynamic [Lewis].} \end{array} \right.$

13. (a) Bevel Gear.  $\left\{ \begin{array}{l} \text{General.} \\ \text{Lewis method.} \end{array} \right.$
- 

(OR)

- Worm Gear  $\left\{ \begin{array}{l} \text{General} \\ \text{Lewis method.} \end{array} \right.$
- 

14. (a) Gear box :-

↳ 6 Speed }  
 ↳ 9 Speed }  $\phi$ , Spindle speed, Ray diagram  
 Structural Formula, Kinematic Arrangement.

(OR)

(b) ↳ 12 Speed Gearbox  
 ↳ 16 Speed " "  
 ↳ 18 Speed " "

15. (a) Clutch  $\left\{ \begin{array}{l} \text{Single plate clutch [Theory/Problems]} \\ \text{Cone " " [Theory/ "]} \\ \text{Multiple " " " " " "} \end{array} \right.$

(OR)

(b) Brake  $\left\{ \begin{array}{l} \text{Single brake (Derivation/Problem)} \\ \text{Double Side " " " " " "} \\ \text{Band Brake.} \end{array} \right.$

(OR)

Cam profile [Rare].

Part - c :-

↳ Expected from UNIT - 4 (OR) UNIT - 5.

Design flat belt drive to transmit 25 kW at 720 rpm to an aluminium rolling machine with a speed reduction of 3.0. The distance between the shaft is 3m, Diameter of rolling machine pulley is 1.2 m.

Given :-

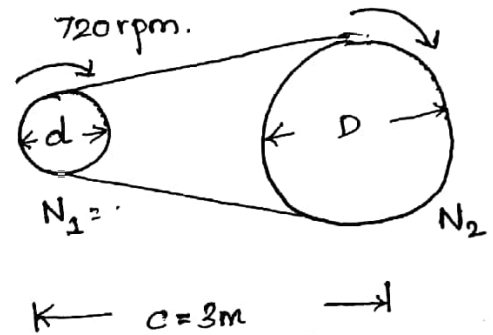
$$\text{Rated Power (P)} = 25 \text{ kW} = 25 \times 10^3 \text{ W}$$

$$\text{Speed Reduction (i)} = 3 \quad (\because N_1/N_2 = i)$$

$$C = 3 \text{ m}$$

$$D = 1.2 \text{ m.}$$

$$N_1 = 720 \text{ rpm.}$$



To find :-

Design Flat belt drive

Solution :-

Step 1 :- Pulley Diameter (d) :-

$$N_1 \times d = N_2 \times D$$

$$\frac{N_1}{N_2} = \frac{D}{d} \quad \because i = \frac{N_1}{N_2} = 3.$$

$$\therefore \frac{D}{d} = 3$$

Here, Driven Pulley diameter (D) = 1.2 m (or) 1200 mm.

$$\therefore d = D : 3.$$

$$d = 400 \text{ mm}$$

From data book, Page No. 7.54, Recommended smaller pulley diameter  $d = 400 \text{ mm}$  (available).



Step 2 :- Design Power ( $D_p$ ):-

$$D_p = \frac{\text{Rated Power (kW)} \times \text{Load Correction Factor (} K_s \text{)}}{\text{Arc of Contact factor (} K_a \text{)} \times \text{Smaller Pulley factor (} K_d \text{)}}$$

$$D_p = \frac{P \times K_s}{K_a \times K_d}$$

✓ Rated Power ~~€ kW~~  $P = 25 \text{ kW}$  (Given).

✓ Load Correction factor ( $K_s$ ):-

For shock  $K_s = 1.5$

(Data book, Page No. 7.53)

From table no. 1.1, For rolling machine, it's on shock load.

So, load  $K_s = 1.5$ .

✓ Arc of Contact factor ( $K_a$ ):-

$$\text{Arc of Contact } (\alpha) = 180 - \left( \frac{D-d}{c} \right) \times 60 \quad \text{(Data book, Page No. 7.54)}$$

$$\alpha = 180 - \left( \frac{1200 - 400}{3000} \right) \times 60$$

$$\alpha = 164^\circ$$

For  $\alpha = 164^\circ$ , table No. 1.2, the arc of contact factor ( $K_a$ ) = 1.06

✓ Smaller Pulley diameter Factor ( $K_d$ ):-

For  $d = 400 \text{ mm}$ , table No.

$$K_d = 0.8$$

$$\therefore D_p = \frac{25 \times 1.5}{1.06 \times 0.8}$$

$$D_p = 44.22 \text{ kW}$$

Step 3 :- Belt Type :

For heavy load ( $P = 25 \text{ kW}$ ), select belt type  $\rightarrow$  Table no. 3.4

FORT DUCK belting  $\leftarrow$

data book, Page no. 7.52  
7.54

Hence, Load Rating capacity at  $10 \text{ m/s} = 0.0289 \text{ kW/mm/ply}$

Step 4 :- Belt Rating or Load Rating :-

Load Rating at  $v \text{ m/s} \Rightarrow$  Load Rating at  $10 \text{ m/s} \times \frac{v}{10}$ .

Where,  
Velocity of belt ( $v$ ) =  $\frac{\pi \times D \times N_2}{60}$  (or)  $\frac{\pi \times d \times N_1}{60} \Rightarrow 15.07 \text{ m/s}$

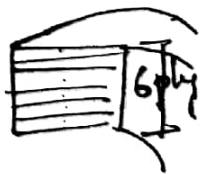
$\therefore$  Load Rating at  $15.07 \text{ m/s} \Rightarrow 0.0289 \times \frac{15.07}{10}$

$= 0.04355 \text{ kW/mm/ply}$

Step 5 :- Width of Belt ( $w$ ) :-

$\checkmark$  From table no. 3.4, For belt velocity ( $15.07 \text{ m/s}$ ) and smaller diameter ( $400$ ). Let us select no. of. Plies as  $6$ .

$\therefore$  Width of belt ( $w$ ) =  $\frac{\text{Design Power } (D_p)}{\text{Load Rating} \times \text{No. of. Plies.}}$



$w = \frac{44.22}{0.04355 \times 6}$

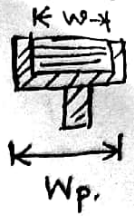
$w = 169.2 \text{ mm}$

$\checkmark$  Select Standard Width, For no. of. plies ( $6$ ), from table no. (Data book, Page no. 7.52).

$w = 180 \text{ mm}$

Step: 6 Pulley Width ( $W_p$ ).

$$W_p = W + (\text{Wider Width})$$



✓ From table no. 1.7 Corresponding width of pulley (180 mm), Wider Width = 25 mm.

$$\therefore \text{Width of Pulley } (W_p) = 180 + 25 = 205 \text{ mm.}$$

Step: 7 Length of belt :- (L)

For open belt drive,

$$L = 2C + \frac{\pi}{4} (D+d) + \left( \frac{D^2 - d^2}{4C} \right)$$

$$= 2(3000) + \frac{\pi}{4} (1200 + 400) + \left( \frac{1200^2 - 400^2}{4(2000)} \right)$$

$$= 6000 + 1256.63 + 106.66$$

$$= 7363.29 \text{ mm}$$

## Problem 2:-

Design of Flat belt drives to transmit 10 kW at 730 rpm of the driver pulley. Speed Reduction is to be 3.5. Driving Assume that the Service is 16 hours a day.

Given :-

Select a flat belt to drive a mill at 230 rpm from a 10 kW, 730 rpm motor. Centre distance is to be around 2 m. The mill shaft pulley is of 1 m diameter.

Given :-

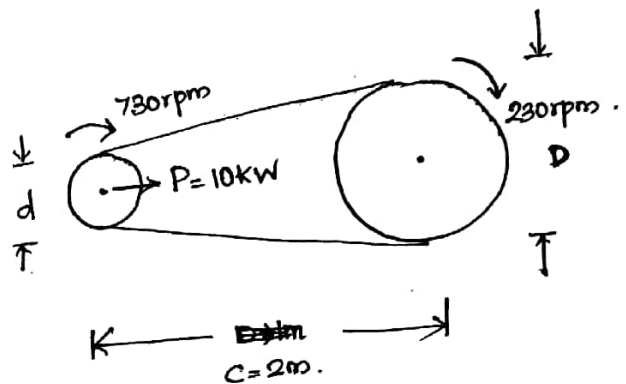
$$\text{Rated Power (P)} = 10 \text{ kW}$$

$$N_1 = 730 \text{ rpm}$$

$$N_2 = 230 \text{ rpm}$$

$$C = 2 \text{ m}$$

$$D = 1 \text{ m}$$



To Find :-

Design flat belt drive.

Solution :-

Step 1 :- Pulley Diameter := (d)

$$N_1 \times d = N_2 \times D$$

$$\frac{N_1}{N_2} \Rightarrow \frac{D}{d}$$

$$\frac{730}{230} = \frac{1000}{d}$$

$$\boxed{d = 315 \text{ mm}}$$

✓ From data book, Page No. 7.54. Recommended Smaller pulley diameter  $d = 315 \text{ mm}$  (Available).

Step 2 :- Design Power ( $D_p$ ) :-

$$D_p = \frac{\text{Rated Power (kW)} \times \text{Load Correction Factor (}k_s\text{)}}{\text{Arc of Contact Factor (}k_\alpha\text{)} \times \text{Smaller Pulley Factor (}k_d\text{)}}$$

✓ Rated Power,  $P \Rightarrow 10 \text{ kW}$

✓ Load Correction Factor ( $k_s$ ) :-

From table no. 1.1, For <sup>mill</sup>Rolling machine, its on Intermediate Load

$$k_s = 1.3 \text{ (Data book, Page No. 7.53).}$$

✓ Arc of Contact factor ( $k_\alpha$ ) :-

$$\alpha = 180 - \frac{(D-d)}{c} \times 60 \text{ (Data book, Page No. 7.54).}$$

$$\alpha = 180 - \left( \frac{1000 - 315}{2000} \right) \times 60.$$

$$\alpha = 159.5^\circ$$

For 159, table no. 1.2, the arc of Contact factor

$$k_\alpha = 1.08$$

✓ Smaller Pulley Diameter Factor ( $k_d$ ) :-

For  $d = 315 \text{ mm}$  table no. 1.3

$$k_d = 0.8$$

$$\therefore D_p \Rightarrow \frac{P \times k_s}{k_\alpha \times k_d}$$

$$\Rightarrow \frac{10 \times 1.3}{1.08 \times 0.8}$$

$$\boxed{D_p \Rightarrow 11.23 \text{ kW}}$$

Step 6:- Pulley Width ( $W_p$ ) :-

$$W_p = W + (\text{Wider Width})$$

✓ From Table no. 1.7, Corresponding Width of pulley (100 mm),  
Wider Width = 13 mm.

$$\therefore \text{Width of Pulley } (W_p) = 100 + 13 = 113 \text{ mm}$$

Step 7:- Length of Belt :- (L)

✓ For Open belt drives,

$$L = 2c + \frac{\pi}{4} (D+d) + \left( \frac{D^2 - d^2}{4c} \right)$$

$$= 2(2000) + \frac{\pi}{4} (1000+315) + \frac{1000^2 - 315^2}{4(2000)}$$

$$\Rightarrow 4000 + 283.75 + 112.59$$

$$L \Rightarrow 4396.34 \text{ mm}$$

Calculate the power capacity of the leather belt of 9mm x 250mm is used to drive a CI pulley 900mm in diameter at 400 rpm. If the active arc on the smaller pulley is  $120^\circ$  and stress in tight side is 2MPa, The density of the leather may be taken as  $980 \text{ kg/m}^3$  and coefficient of friction of leather on CI is 0.35

Given :-

$$d = 900 \text{ mm}$$

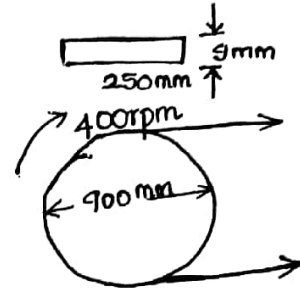
$$N = 400 \text{ rpm}$$

$$\alpha = 120^\circ = 120 \times \frac{\pi}{180} \Rightarrow 2.094 \text{ rad}$$

$$\sigma = 2 \text{ MPa}$$

$$\rho = 980 \text{ kg/m}^3$$

$$\mu = 0.35$$



To find :-

Power Capacity (P) = ?

Solution:

Power Transmitted by belt :-

$$P = (T_1 - T_2) v$$

Tension Ratio,

$$\frac{T_1}{T_2} = e^{\mu \alpha}$$

$$\frac{T_1}{T_2} = e^{0.35 \times 2.094}$$

$$\frac{T_1}{T_2} = 1.87$$

$$\boxed{T_1 = 1.87 T_2} \quad \text{--- equ (1)}$$

We know that,

$$\text{Maximum Tension (T)} = \sigma \times b \times t$$

$$= 2 \times 10^6 \times 9 \times 10^{-3} \times 0.250$$

$$T_1 = 4500 \text{ N}$$

Sub  $T_1$  in equ<sup>n</sup> (1)

$$4500 = 1.87T_2$$

$$T_2 = \frac{4500}{1.87}$$

$$T_2 = 2406.41 \text{ N}$$

∴ Power Transmission,  $P = (T_1 - T_2)v$

$$P = (4500 - 2406.41) 18.84$$

$$P \Rightarrow 39.44 \text{ kW}$$

$$\begin{aligned} \therefore v &= \frac{\pi dN}{60} \\ &= \frac{\pi \times 0.9 \times 400}{60} \\ &= 18.84 \text{ m/s.} \end{aligned}$$



A flat belt drive is required to transmit 12 kW from a motor running at 720 rpm. The belt is 12 mm thick and has mass density of  $0.001 \text{ gm/mm}^3$ . Permissible stress in the belt not to exceed  $2.5 \text{ N/mm}^2$ . Diameter of driving pulley is 250 mm whereas the speed of driven pulley is 240 rpm. The two shafts are 1.25 m apart, coefficient of friction is 0.25. Determine the width of the belt.

Problem

The following data relates to a flat drive.

Power Transmitted = 20 kW

Pulley diameter = 1.8 m

Angle of Contact =  $180^\circ$

Speed of Pulley = 400 rpm

Co-efficient of friction between pulley and belt = 0.35

Permissible Stress for belt =  $300 \text{ N/cm}^2$

Thickness of belt = 8 mm

Density of the belt material =  $950 \text{ kg/m}^3$

Determine the width of the ~~pulley~~ belt required taking Centrifugal tension.

Given :-

$P = 20 \text{ kW}$ ,  $D = 1.8 \text{ m}$ ,  $\alpha = 180^\circ = 180 \times \frac{\pi}{180} = 2.79 \text{ rad}$ ,  $N = 400 \text{ rpm}$ .

$\mu = 0.35$ ,  $\sigma = 300 \text{ N/cm}^2$ ,  $t = 8 \text{ mm}$ ,  $\rho = 950 \text{ kg/m}^3$ .

To find :-

$b = ?$

Solution :-

✓ Power Transmitted by belt;

$$P = (T_1 - T_2) v$$

Where,  $v = \pi d N / 60 = 37.69 \text{ m/s}$ .

$$20 \times 10^3 = (T_1 - T_2) 37.69$$

$$T_1 - T_2 = 530.51 \quad \text{--- --- --- (1)}$$

Flat belt tension,  $T_1$

$$\frac{T_1}{T_2} = e^{\mu \alpha}$$

$$\frac{T_1}{T_2} = e^{0.35 \times 2.79}$$

$$T_1 = 2.65 T_2 \quad \text{--- (2)}$$

Sub (2) in (1), We get

$$2.65 T_2 - T_2 = 530.51$$

$$T_2 = 321.52 \text{ N-m.}$$

$$\therefore T_1 = 852.03 \text{ N-m}$$

Maximum Tension in the belt,  $T \leq \sigma \cdot A \rightarrow T_c$

$$T_1 = \sigma \cdot A + T_c$$

$$852.03 = 300 \times 10^4 \times (b \times t) + T_c$$

✓ Area of Cross-section of belt (A) =  $b \times t$   
=  $b \times 8$   
=  $8b \times 10^{-6} \text{ mm}^2$

✓ Centrifugal Tension ( $T_c$ ):-

$$T_c = m \cdot v^2$$

$$= (p \times A \times L) \times v^2$$

$$\Rightarrow 980 \times 8b \times 10^{-6} \times (37.69)^2$$

$$\Rightarrow 11.137b$$

$$(\because m = p \times v)$$

$$852.03 = 300 \times (8b \times 10^{-6}) + 11.137b$$

$$852.03 = 2.4 \times 10^{-3} b + 11.137b$$

$$b = 76.48 \text{ mm.}$$

Standard Width,  $b = 90 \text{ mm}$

## Problem:- 1

A 50kW motor running at 1000rpm. is required to drive a pump pulley at 400rpm. The motor pulley diameter is limited to 0.3m. Centre distance around 2.5m. Select suitable V-belt and design V-belt.

Given :-

$$P = 50 \text{ kW}$$

$$N_1 = 1000 \text{ Rpm}$$

$$N_2 = 400 \text{ rpm}$$

$$d = 0.3 \text{ m} = 300 \text{ mm}$$

$$C = 2.5 \text{ m} \Rightarrow 2500 \text{ mm.}$$

To find :-

Design V-belt drives.

Solution :-

Step 1 :- Selection of V-Belt;

✓ Based on power transmission ( $P=50\text{KW}$ ), select V-belt section from table no. 1.12 (Data book, Page No. 7.58).

C-section is selected

Step 2 :- Pulley Diameter ( $D$  &  $d$ ) :-

✓ To find pulley diameter ( $D$ ), by using relation,

$$\frac{N_1}{N_2} = \frac{D}{d}$$

$$\frac{1000}{400} = \frac{D}{300}$$

$$D = 750 \text{ mm.}$$

✓ Select standard pulley diameter (driven) from table no. 1.0

$$D = 800 \text{ mm}$$

Step 3:

Determine the centre distance:-

To determine the centre distance from the table no. 1.15 but here centre distance is given. " $C = 2500\text{mm}$ ".

Step 4:

Calculation of design power ( $D_p$ )

$$D_p = \frac{\text{Rated Power (Kw)} \times \text{Service Factor (F}_a)}{\text{Arc of Contact factor (F}_d) \times \text{Length Correction factor (F}_l)}$$

✓ Rated Power = 50 Kw (Given).

✓ Service factor ( $F_a$ ):-

Select Service factor from table no. 1.13 based on application. (pump)  
So,  $F_a = 1.3$  (assume 16 hrs/day).

✓ Arc of Contact factor ( $F_d$ ):-

$$\begin{aligned} \text{Arc of Contact} &= 180 - \left(\frac{D-d}{C}\right) \times 60 \\ &= 180 - \left(\frac{800-300}{2500}\right) \times 60 \end{aligned}$$

$$\alpha = 168^\circ$$

For  $168^\circ$ , From table no. 1.16

$$F_d \Rightarrow 0.97$$

✓ Length Correction Factor ( $F_l$ )

✓ Calculate the length Using relation

$$L = 2C + \pi/2 (D+d) + \frac{(D-d)^2}{4C}$$

$$L = 2(2500) + \frac{\pi}{2} (800+300) + \frac{(800-300)^2}{4 \times 2500}$$

$$= 5000 + 1727.87 + 25 = 6752.87 \text{ mm.}$$

From data book, Page No. 7.60, standard Nominal inside length is 6807, corresponding c-section belt length and length correction factor are 6863 mm & 1.14.

$$L = 6863 \text{ mm}$$

$$F_c = 1.14.$$

$$\therefore D_p = \frac{50 \times 1.3}{0.97 \times 1.14} = 51.09 \text{ kW}$$

Step 5 :- Calculate Maximum Power Capacity :-

✓ For V-belt, "C" section, max. power capacity from table No. "1-14"

$$d_w = \left( 1.475^{-0.09} - \frac{142.7}{d_e} - 2.34 \times 10^{-4} d_e^2 \right) S.$$

Where,

$d_e =$  Equivalent pitch diameter  $\therefore d_e = d_p \times F_b$

Note

$F_b$  value taken from table <sup>data book page "7.62"</sup> or using formula  $d_e = d_p \times F_b$ .

Here,  $d_e = d_p \times F_b$   $\therefore d_p = 300 \text{ mm}$  (smaller pulley diameter).  
 $F_b = 1.13$  (DB. Page no. 7.62).

$$\therefore d_e = 339 \text{ mm}$$

S - Speed of belt

$$\therefore \frac{\pi d N_1}{60} = \frac{150000 \text{ mm}}{60}$$

$$S = \frac{\pi \times 0.3 \times 1000}{60} = 15.707 \text{ m/s.}$$

$$\therefore k_w = \left( 1.47 (15.707)^{-0.09} - \frac{142.7}{339} - 2.34 \times 10^{-4} (15.707)^2 \right) 15.707$$

$$k_w = (1.147 - 0.420 - 0.057) 15.707 \Rightarrow 10.52 \text{ kW.}$$

Step 6: No. of belt ( $n_b$ ):

$$n_b = \frac{\text{Design Power } (D_p)}{\text{Maximum Power Capacity } (k_w)}$$

$$n_b = \frac{51.09}{10.52} \approx 4.98 \approx 5 \text{ belts}$$

Step 7: Corrected Centre distance (C):

✓ Centre distance corrected by,

$$C_{\text{actual}} = A + \sqrt{A^2 - B}$$

Where,

$$A = \frac{L}{4} - \pi \left( \frac{D+d}{8} \right)$$

$$\Rightarrow \frac{6863}{4} - \pi \left( \frac{200+300}{8} \right) \Rightarrow 1285.28$$

$$B = \frac{(D-d)^2}{8} = 31250$$

$$\therefore C_{\text{actual}} = 1285.28 + \sqrt{1285.28^2 - 31250} \Rightarrow 2558 \text{ mm}$$

# Problem 2

A Centrifugal pump running at 340 rpm is to be driven by a 100 kW motor running at 1440 rpm. The drives is to work for atleast 20 hrs every day. The Centre distance b/w the motor shaft and the pump shaft is 2000 mm. Suggest a suitable V-belt.

Solution :-

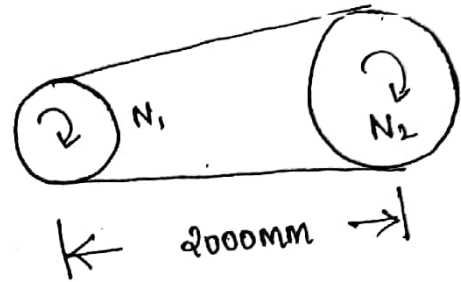
$$P \Rightarrow 100 \text{ kW}$$

$$N_1 \Rightarrow 1440 \text{ rpm}$$

$$N_2 = 340 \text{ rpm}$$

$$C = 2000 \text{ mm}$$

$$\text{Duty} \Rightarrow 20 \text{ hrs/day}$$



To find: Suggest suitable V-belt

Solution :-

Step 1:- Selection of V-belt :-

✓ Based on the power transmission ( $P=100 \text{ kW}$ ), select V-belt section from table no. 1.12 (Data book, Page No. 7.58).

D-section is selected

Step 2:- Pulley Diameter ( $d$  &  $D$ )

✓ Here smaller pulley diameter pulley is not given, take diameter from table no. 1.12 based on the V-belt section (D)

For 'D'-section,  $d = 355 \text{ mm}$

$$\frac{N_1}{N_2} = \frac{D}{d}$$

$$\frac{1440}{340} = \frac{D}{355}$$

$$\therefore D = 1503 \text{ mm}$$

✓ Select Standard pulley diameter from table no. 1.10  
Data book, page no. 7.54

$$D = 1120 \text{ mm.}$$

Step 3:- Centre distance:

$$C = 2000 \text{ mm [given].}$$

Step 4:- Design power ( $D_p$ ):

$$D_p = \frac{\text{Rated Power} \times \text{Service factor}}{\text{Arc of contact factor} \times \text{Length correction factor.}}$$

✓ Rated Power  $\Rightarrow$  100kW.

✓ Service factor ( $F_a$ ):-

✓ For 20 hrs/day, ( $F_a$ ) = Service factor from table no. 1.13  
based on the application (pump).

$$F_a = 1.4$$

✓ Arc of Contact factor ( $F_\alpha$ ).

$$\alpha = 180 - \left( \frac{D-d}{c} \right) \times 60.$$

$$\alpha = 180 - \left( \frac{1120 - 355}{2000} \right) \times 60.$$

$$\alpha = 157^\circ.$$

For,  $157^\circ$ , from table no. 1.16

$$F_d = 0.94$$



Length Correction factor ( $F_c$ ):

✓ Calculate the length Using Relation,

$$L = 2C + \frac{\pi}{2}(D-d) + \frac{(D-d)^2}{4C}$$

$$L = 2(2000) + \frac{\pi}{2}(1120-355) + \frac{(1120-355)^2}{4(2000)}$$

$$= 4000 + 1201.65 + 73.15 \Rightarrow 5274.80 \text{ mm.}$$

✓ From data book, Page No. 7.64, Standard Nominal Inside length is 5334 mm, Corresponding D-Section belt length and length Correction factor are 5413 mm and 0.96.

$$L = 5413$$

$$F_c = 0.96.$$

$$\therefore D_p = \frac{100 \times 1.4}{0.94 \times 0.96} \Rightarrow 155.14 \text{ kW.}$$

Step 5:- Calculation of Maximum Power Capacity

✓ For V-belt "D"-Section maximum Capacity from table no. "1.14"

$$K_w = \left[ 3.225^{-0.09} - \frac{506.7}{d_e} - 4.78 \times 10^{-4} S^2 \right] S.$$

Note :-  $d_e$  Value taken from <sup>data book page 7.62</sup> ~~table~~ no. (or) Using formula  $d_e = d_p \times F_b$

$\therefore F_b = \sqrt{\frac{D}{d}} = \sqrt{\frac{1120}{355}}$  ratio taken by speed ratio ( $\frac{D}{d}$ ) from table

data book, Page No. 7.62.

$$F_b = 1.14 \quad [\because \frac{D}{d} = 3.14]$$

$$\therefore d_e \Rightarrow 404 \text{ mm.}$$

$$K_w = 3.22 (19.92)^{-0.09}$$

$$S = \frac{\pi D N_2}{60} = \frac{\pi \times 1120 \times 34}{60} \Rightarrow 19.92 \text{ m/s}$$

$$K_w = \left[ 3.22 (19.92)^{-0.09} - \frac{506.7}{404} - 4.78 \times 10^{-4} (19.92)^2 \right] 19.92$$

$$\Rightarrow \left[ \begin{matrix} 2.45 & -0.189 \\ \cancel{0.887} & -1.254 & -0.1900 \end{matrix} \right] 19.92$$

$$K_w = 20.05 \text{ kW}$$

Step 6:- No. of belt ( $n_b$ ):-

$$n_b = \frac{\text{Design Power } (D_p)}{\text{Maximum Power Capacity } (k_w)}$$

$$\Rightarrow \frac{155.14}{20.05} = 7.73 \approx 8 \text{ "8 belt"}$$

Step 7:- Corrected Centre distance (C):-

✓ Centre distance Corrected by,

$$C_{\text{actual}} \Rightarrow A + \sqrt{A^2 - B}$$

Where,

$$A = \frac{L}{4} - \frac{\pi (D+d)}{8}$$

$$= \frac{5413}{4} - \pi \left( \frac{1120+355}{8} \right) \Rightarrow 774.32$$

$$B = \frac{(D-d)^2}{8}$$

$$= \frac{(1120-355)^2}{8} \Rightarrow 73153.125$$

$$\therefore C_{\text{actual}} = 774.32 + \sqrt{(774.32)^2 - 73153.12}$$

$$\Rightarrow 1499.86 \text{ mm}$$

Problem :- 3

A V-belt drives to transmit 45 kW in a heavy duty saw mill which works in two shifts of 8 hours each. The speed of motor shaft is 1400 rpm with the approximate speed reduction of 3 in the machine shaft. Design the drive and calculate the average induced stress in the belt.

Given :-

$$P = 45 \text{ kW}$$

$$N_1 = 1400 \text{ rpm}$$

$$i = 3$$

Service duty = 16 hrs/day (Heavy duty).

To find :-

- ✓ Design drives
- ✓ Average stress.

Solution :-

Step 1 :- Selection of V-belt :-

✓ Based on the power transmission ( $P = 50 \text{ kW}$ ), select V-belt selection from table no. 1.12 (Data book, Page No. 7.58).

"c-section" is selected

Step 2 :- Pulley Diameter :- ( $d$  &  $D$ )

✓ Here smaller pulley diameter is not given, diameter from table no. based on the V-belt section, for c-section  $d = 200 \text{ mm}$

$$\frac{N_1}{N_2} = \frac{D}{d}$$

$$\therefore \frac{N_1}{N_2} = 3$$

$$3 = \frac{D}{200}$$

$$D = 600 \text{ mm}$$

✓ Select standard pulley diameter from table no. 1.0 (Pg. DB: 7.54)

Step 3:- Centre distance

✓ To determine the Centre distance from table no. "1.15"

Here,  $D/d = 3$ , corresponding  $D/d$  ratio,  $C/D \approx 1.0$ .

$$\frac{C}{630} = 1$$

$$\therefore C = 630 \text{ mm.}$$

Step 4:- Design Power ( $D_p$ ):-

$$D_p = \frac{\text{Rated Power (kW)} \times \text{Service Factor (F}_a\text{)}}{\text{Arc Of Contact factor (F}_\alpha\text{)} \times \text{Length Correction Factor (F}_L\text{)}}$$

✓ Rated Power (kW):-

$$P = 50 \text{ kW}$$

✓ Service Factor ( $F_a$ ):-

✓ For 2 shifts / day and heavy duty saw mills: From table no. "1.13"

$$F_a = 1.3$$

✓ Arc Of Contact factor ( $F_\alpha$ ):- From Data book. 7.68.

$$\alpha = 180 - \left( \frac{D-d}{C} \right) \times 60.$$

$$= 180 - \left( \frac{630 - 200}{630} \right) \times 60$$

$$= 139^\circ$$

From table no. "1.16" corresponding  $\alpha = 139^\circ$ .

$$F_\alpha = 0.89.$$

Length Correction factor ( $F_c$ ):

✓ Calculate the length Using Relation,

$$L = 2C + \frac{\pi}{2}(D+d) + \frac{(D-d)^2}{4C}$$

DB, Page No. 7.61.

$$= 2(630) + \frac{\pi}{2}(630+200) + \frac{(630-200)^2}{4(630)}$$

$$\Rightarrow 2637.13 \text{ mm}$$

✓ From DB, Page No. 7.64, Standard Nominal inside length is 2667, Corresponding c-section, d

$$\text{Belt length } (L) = 2723 \text{ mm}$$

$$F_c = 0.94$$

$$\therefore D_p = \frac{50 \times 1.3}{0.89 \times 0.94} = 77.69 \text{ kW}$$

Step 5 :- Maximum Power Capacity

✓ For V-belt "C" - Section, Maximum Power Capacity from Table no. "1, 14"

$$K_w = \left[ 1.47s^{-0.09} - \frac{142.7}{d_e} - 2.34 \times 10^{-4} s^2 \right] s$$

Where,

$$s \Rightarrow \frac{\pi \times N_s \times d}{60} \Rightarrow \frac{\pi \times 1400 \times 0.200}{60} = 14.66 \text{ m/s}$$

$d_e \Rightarrow d_p \times F_b$ , from data book, page no. 7.62 corresponding  $D/d$  ratio  $F_b = 1.14$   $\therefore d_e = d$

$$d_e = 200 \times 1.14 = 228 \text{ mm}$$

$$\therefore P_w = \left( 3.47 (14.66)^{-0.09} - \frac{142.7}{208} - 2.34 \times 10^{-4} (14.66)^2 \right) 14.66$$

$$= (1.154 - 0.625 - 0.050) 14.66$$

$$P_w \Rightarrow 7.02 \text{ kW}$$

Step 6:- Number of belt ( $n_b$ ):

$$n_b = \frac{\text{Design Power (Dp)}}{\text{Maximum Power Capacity (kW)}}$$

$$= \frac{77.69}{2.02} \approx 12 \text{ belts}$$

Step 7:- Corrected Centre distance (C).

✓ Centre distance corrected by,

$$C_{\text{actual}} = A + \sqrt{A^2 - B}$$

Where,

$$A \Rightarrow \frac{L}{4} - \frac{\pi(D+d)}{8}$$

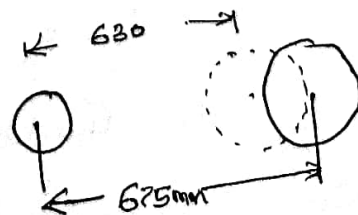
$$\Rightarrow \frac{2723}{4} - \frac{\pi(630+200)}{8}$$

$$\Rightarrow 680.75 - 325.94 = 354.80$$

$$B = \frac{(D-d)^2}{8} = \frac{(630-200)^2}{8} = 23112.5$$

$$\therefore C_{\text{actual}} = 354.80 + \sqrt{(354.80)^2 - 23112.5}$$

$$C_{\text{actual}} \Rightarrow 675 \text{ mm}$$

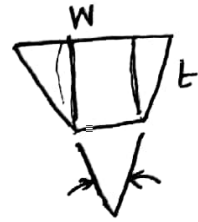


∴ Average Induced stress in the belt :-

$$\text{Stress} \Rightarrow \frac{\text{Maximum Tension}}{\text{Cross-sectional Area.}}$$

Here, Cross-sectional area of "C-section"

$$A = 230 \text{ mm}^2$$



Maximum tension :-

W.K. that,

$$P = (T_1 - T_2)v$$

$$450 \times 10^3 = (T_1 - T_2)14.66 \quad (\because v = 14.66 \text{ m/s})$$

$$T_1 - T_2 = 3069.57 \quad \text{--- (1)}$$

Belt tension ratio,

$$\frac{T_1}{T_2} = e^{\mu \alpha \operatorname{cosec} \beta}$$

Where,

$$\mu = 0.3 \text{ (Assume).}$$

$$2\beta = 35^\circ, \beta = 17.5^\circ$$

$\alpha$  = Wrap angle (or) Arc of contact in rad.

$$\alpha = 139^\circ \text{ (or) } 2.44 \text{ rad.}$$

$$\therefore \frac{T_1}{T_2} = e^{0.3 \times 2.44 \times \frac{1}{\cos 17.5}}$$

$$\frac{T_1}{T_2} = 2.15 \quad \text{--- (2)}$$

$$T_1 = 2.15T_2 \quad \text{--- (2)}$$

Design a v-belt drive to transmit 50 kW at 1440 rpm from an electric motor to a textile machine running 24 hrs a day. The speed of the machine shaft is 480 rpm.

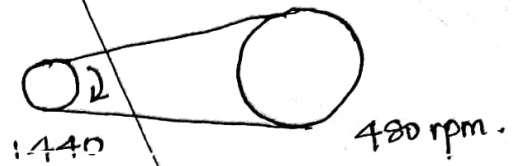
Given :-

$$\text{Power (P)} = 50 \text{ kW}$$

$$N_1 = 1440 \text{ rpm}$$

$$N_2 = 480 \text{ rpm}$$

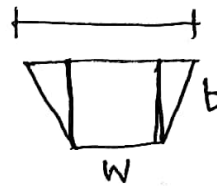
$$\text{Service duty} = 24 \text{ hrs/day.}$$



To find : Design V-belt.

Solution :-

Step 1 :- Selection of v-belt :-



Sub equ<sup>n</sup> (2) in (1)

$$\therefore 2.15 T_2 - T_2 = 3069.57$$

$$T_2 = 2669.19 \text{ N}$$

$$\text{Sub: } T_2 = 2669.19 \text{ in equ<sup>n</sup> (or) equ<sup>2</sup>}$$

$$T_1 = 2.15 T_2$$

$$T_1 = 5738.75 \text{ N}$$

Here,  $T_1 = 5738.75$  is maximum tension :

$$\therefore \text{Stress} = \frac{5738.75}{230} = 24.95 \text{ N/mm}^2$$



## Chain drive :-

↳ Given data :-

$$P = 50 \text{ kW}$$

$$N_1 = 1000 \text{ Rpm}$$

$$N_2 = 300 \text{ Rpm}$$

$$a_0 = 500 \text{ mm}$$

Procedure :-

1. Transmission Ratio :-

$$i = \frac{N_1}{N_2} = \frac{Z_2}{Z_1}$$

$$i = 1000/300 = 2.85$$

$$\boxed{\text{Std } i = 3.15}$$

2. No. of teeth in Sprockets :-  $Z_1$  &  $Z_2$

↳ Based 'i' Value

$$Z_1 = 27$$

$$Z_2 = i \times 27 = 78$$

3. Standard Pitch :- (P)

$$a = (30 \text{ to } 50)P$$

$$a = 30P, a = 50P$$

$$P_{\text{max}} = 500/30, P_{\text{min}} = 500/50$$

$$P_{\text{max}} = 16.6 \text{ mm}, P_{\text{min}} = 10 \text{ mm}$$

$$\text{Standard pitch, } P = 15.875 \text{ mm}$$

4. Chain Selection :- (7.71 to 7.73)

↳ Sel. chain based on standard pitch,

10A-2/DR50

↳ Bearing Area =  $1.40 \text{ cm}^2$

↳ Weight =  $17.8 \text{ N}$

↳ Breaking Load =  $44400 \text{ N}$ .

5. Total Load :- ( $P_T$ ) (7.78)

$$P_T = P_t + P_c + P_s$$

$$\text{↳ } P_t = \frac{1020}{v} \times N$$

$$\Rightarrow 7139.10 \text{ N}$$

$$\because N = \text{KW}$$

$$v = \frac{z_1 \times P_1 \times N_1}{60 \times 1000}$$
$$= 7.14 \text{ m/s.}$$

$$\text{↳ } P_c = m v^2$$

$$\Rightarrow 1.78 \times 7.14^2$$

$$\Rightarrow 90.74 \text{ N}$$

$$\text{↳ } P_s = k \cdot W \cdot a$$

$$\Rightarrow 6 \times 17.8 \times 0.500$$

$$\Rightarrow 107.3 \text{ N.}$$

$$\therefore P_T = 7139.10 + 90.74 + 107.3$$

$$\boxed{P_T \Rightarrow 7340.89 \text{ N}}$$

6. Service Factor :-  $K_s$ .

$$K_s = k_1 \cdot k_2 \cdot k_3 \cdot k_4 \cdot k_5 \cdot k_6$$

$$\boxed{K_s = 1.5}$$

7. Design load :-  $D_L$

$$D_L = P_T \times K_s.$$

$$= 7340 \times 1.5$$

$$\boxed{D_L = 11.05 \text{ KN}}$$

8. FOS :-

$$F_{sw} = \frac{\text{Breaking Load}}{D_L}$$

$$\Rightarrow \frac{44400}{11.05 \times 10^3}$$

$$\boxed{F_{sw} = 4.08}$$

9. Bearing Stress :-  $\sigma_b$

$$\rightarrow \sigma_b = \frac{D_L}{\text{Area}}$$

$$= \frac{11.05 \times 10^3}{1.40}$$

$$\Rightarrow 7.86 \text{ N/cm}^2$$

10. Length of the chain :-

$$\rightarrow L = l_p \cdot P$$

$$L_p = 2a_p + \left(\frac{z_1 + z_2}{2}\right) + \frac{(z_2 - z_1)}{2\pi}$$

$a_p$

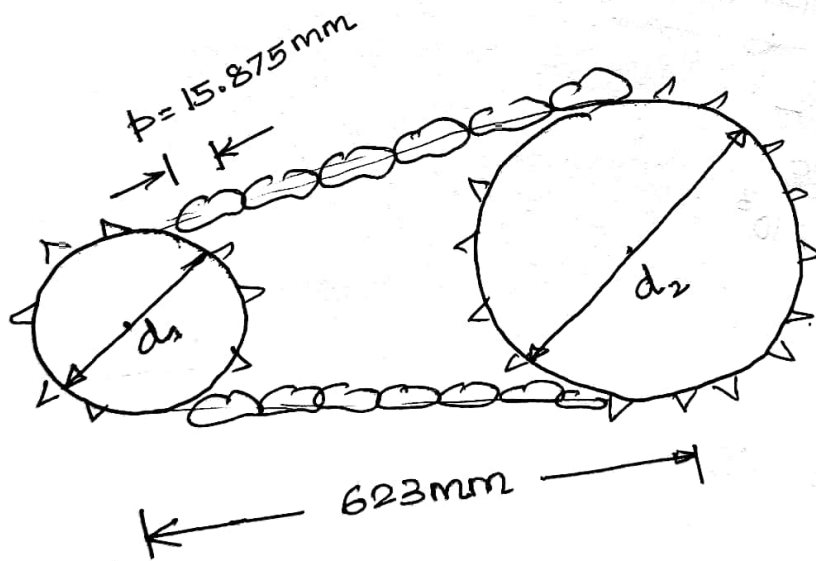
$$\Rightarrow 116 \text{ [EVEN]}$$

$$\therefore L = 1860 \text{ mm}$$

12. Exact Centre distance :-

$$a = \frac{e + \sqrt{e^2 - 8m \cdot p}}{4} \cdot p$$

$$\boxed{a = 623 \text{ mm}}$$



Spur Gear And Helical Gear.

1. Design Of Spur Gear Drive To Transmit 22.5 kW At 900 rpm. Speed Ratio is 2.5. Material for Pinion and Wheel are C45 Steel. Working life = 10,000 hrs.

Given Data :-

$$\begin{aligned} \rightarrow P &= 22.5 \text{ kW} \\ N_1 &= 900 \text{ rpm} \\ i &= 2.5 \\ \phi &= 20^\circ \\ N &= 10,000 \text{ hrs.} \end{aligned}$$

1. Material Selection :-

Pinion / Gear  $\Rightarrow$  C45 Steel

2. Compressive Stress & Bending Stress :-  $[\sigma_c]$  &  $[\sigma_b]$

$$[\sigma_b] = \frac{1.4 \text{ K}_{\text{v}} \sigma_{-1}}{n K_{\sigma}}$$

$$\rightarrow \sigma_{-1} = 0.25 [\sigma_u + \sigma_y] + 50$$

$$\sigma_u = 490 \text{ N/mm}^2, \sigma_y = 240 \text{ N/mm}^2$$

$$\therefore \sigma_{-1} = 232.5 \text{ N/mm}^2$$

$$\rightarrow n = 2.0$$

$$\rightarrow k_{\sigma} = 1.2 \text{ [Case Hardened]}$$

$$\therefore [\sigma_b] = \frac{1.4 \times 1 \times 232.5}{2 \times 1.2}$$

$$\boxed{[\sigma_b] \Rightarrow 135.625 \text{ N/mm}^2}$$

$$[\sigma_c] = C_R \cdot HRC \cdot k_{ct}$$

$$\rightarrow C_R = 220$$

$$\rightarrow HRC = 63$$

$$\rightarrow k_{ct} = 0.585$$

$$\therefore [\sigma_c] = 220 \times 63 \times 0.585$$

$$\boxed{[\sigma_c] = 810.81 \text{ N/mm}^2}$$

3. Min. Centre Distance :-

$$a \geq (i+1) \sqrt[3]{\frac{(0.74)^2 \cdot E [M_T]}{[\sigma_c] \cdot i \psi}}$$

$$\rightarrow E = 2.15 \times 10^5 \text{ N/mm}^2$$

$$\rightarrow [M_T] = T \cdot k \cdot k_d$$

$$[M_T] \Rightarrow 239.73 \text{ N/mm}^2$$

$$\rightarrow \psi \Rightarrow 0.3$$

$$T = \frac{60 \times P}{2\pi N_1}$$

$$T = 239.73 \text{ N/mm}^2 \times 1.3.$$

$$\therefore a \geq 135.94 \approx 136 \text{ mm.}$$

4. Module :- (m)

$$m \geq 1.26 \sqrt[3]{\frac{[M_T]}{\gamma \cdot [\sigma_b] \psi_m z_1}}$$

$$\rightarrow \gamma = 0.377$$

$$\rightarrow z_1 = 18$$

$$\rightarrow \psi_m = 10$$

$$\therefore m \geq 4.07 \text{ mm}$$

$$\boxed{m = 5 \text{ mm}} \quad [8.2]$$

5. Connected No. of Teeth :- (8.22)

$$z_1 = \frac{2a}{m(i+1)}$$

$$\Rightarrow \frac{2 \times 136}{5(2.5+1)}$$

$$\boxed{z_1 \Rightarrow 16 \text{ teeth}}$$

$$z_2 = i \times z_1$$

$$\boxed{z_2 \Rightarrow 40 \text{ teeth}}$$

6. Actual Centre Distance :-

$$a = \frac{m(Z_1 + Z_2)}{2}$$

$$a \Rightarrow 140 \text{ mm}$$

7. Pitch dia, Velocity & Facewidth :-

$$\rightarrow d_1 = m \times Z_1 \Rightarrow 5 \times 16 = 80 \text{ mm}$$

$$d_2 = m \times Z_2 \Rightarrow 5 \times 40 = 200 \text{ mm}$$

$$\rightarrow b = \psi \times a \Rightarrow 0.3 \times 140 = 42 \text{ mm}$$

$$b = \psi_m \times m \Rightarrow 10 \times 5 = 50 \text{ mm}$$

$$8. \rightarrow v = \frac{\pi \times d_1 \times N_1}{60 \times 1000} = 6.03 \text{ m/s.}$$

8. Actual Torque :-

$$\rightarrow (M_T) = I. k. k_d$$

$$(M_T) = 242. \text{ N-mm}$$

$$k = 1.02 \quad (8.15)$$

$$k_d = 1.3.$$

9. Checking Compressive and Bending Stress :-

$$(\sigma_c) = 0.74 \frac{(i+1)}{a} \sqrt{\frac{i+1}{ib}} \cdot E \cdot [M_T]$$

$$(\sigma_c) \Rightarrow 711.05 \text{ N/mm}^2 \leq 810.81 \text{ N/mm}^2$$

$\therefore$  Hence is Safe

$$(\sigma_b) = \frac{(i+1)}{a.m.b.y} (M_T) \leq [\sigma_b]$$

$$\Rightarrow 87.42 \text{ N/mm}^2 \leq 135.625 \text{ N/mm}^2$$

$\therefore$  Hence is Safe.



## 10. Parameters :-

1.  $m \Rightarrow 5 \text{ mm}$

2. Add  $\Rightarrow f_o \times m \Rightarrow 1 \times 5 \Rightarrow 5 \text{ mm}$

3. Ded  $\Rightarrow (f_o + c) m \Rightarrow (1 + 0.25) \times 5 \Rightarrow 6.25 \text{ mm}$

4. Working depth  $\Rightarrow 2 \times \text{Add} \Rightarrow 10 \text{ mm}$ .

2. Design of Spur gear drives required to transmit 45 kW at a pinion speed of 800 rpm. The velocity ratio is 3.5:1. The teeth are  $20^\circ$  FD involute with 18 teeth. Both pinion and gear made up of steel with static load  $180 \text{ N/mm}^2$ . Assume medium shock load.

Given :-

$P \Rightarrow 45 \text{ kW} = 45 \times 10^3 \text{ N}$

$N_1 \Rightarrow 800 \text{ rpm}$

$i \Rightarrow 3.5$

$\phi \Rightarrow 20^\circ$

$Z_1 \Rightarrow 18$

$[\sigma_b] \Rightarrow 180 \text{ N/mm}^2$

Sol :-

1. Material Selection :-

$\rightarrow$  Pinion & Gear - Steel

2. No. of teeth :-

$\rightarrow z_1 = 18, z_2 = i \times 18$

$= 3.5 \times 18$

$\Rightarrow 63 \text{ teeth}$ .

3. Tangential load on teeth :-

$$F_T = \frac{P \times K_o}{v}$$

$$F_T = \frac{45 \times 10^3 \times 1.25}{\frac{\pi \times m \times z_1 \times N_1}{60 \times 1000}}$$

$$\Rightarrow 89641.43/m$$

SHOCK	$K_o$
Steady	1.0
Light	1.25
Medium	1.5
Heavy	2.0

4. Initial Dynamic Loading ( $F_d$ )

$$F_d \Rightarrow F_T \times C_v$$

$$\Rightarrow \frac{89641.43}{m} \times 3$$

$$\Rightarrow \frac{268.9 \times 10^3}{m}$$

$$C_v = \frac{6 + v_m}{6} \quad \because v_m = 12 \text{ m/s}$$

$$C_v = 3$$

5. Beam Strength :- ( $F_s$ )

$$F_s \Rightarrow \pi \times m \times b \times [\sigma_b] \times y$$

$$\Rightarrow \pi \times m \times 10m \times 180 \times 0.103$$

$$F_s \Rightarrow 582.54 m^2$$

$$y = 0.154 - \frac{0.912}{z_1}$$

$$y \Rightarrow 0.103$$

6. Module :- ( $m$ )

$$F_d = F_s$$

$$\frac{268.92 \times 10^3}{m} \Rightarrow 582.45 m^2$$

$$m \Rightarrow 7.72 \text{ mm} \approx 8 \text{ mm}$$

7. Pitch diameter ( $d_1$ ), Velocity ( $v$ ) & Facewidth ( $b$ ) :-

$$\begin{aligned} \rightarrow d_1 &= mZ_1, \quad d_2 = mZ_2 \\ &\Rightarrow 8 \times 18, \quad d_2 = 8 \times 63 \\ &\Rightarrow 144 \text{ mm} \quad \Rightarrow 480 \text{ mm} \end{aligned}$$

$$\rightarrow b \Rightarrow 10m \Rightarrow 10 \times 8 \Rightarrow 80 \text{ mm}$$

$$\rightarrow v \Rightarrow \frac{\pi \times d_1 \times N_1}{60 \times 1000} \Rightarrow 6.03 \text{ m/s.}$$

8. Re-calculation of beam strength :- (8.51)

$$F_d = F_T + \frac{0.164 V_m [C_b + F_T]}{0.164 V_m + 1.52 \sqrt{C_b + F_T}}$$

$$C = 11860e$$

$$e = 0.038$$

$$\boxed{F_d \Rightarrow 11345.80 \text{ N}}$$

9. Max. wear load :-

$$F_w = d_1 \times Q \times k \times b$$

$$\boxed{F_w \Rightarrow 6249.6 \text{ N}}$$

$$Q = \frac{2i}{i+1} = 1.5$$

$$k = 0.35$$

10. Check for beam strength :-

$$F_s > F_d$$

$\therefore$  Design is safe

11. Check for wear load :-

$$F_w > F_d$$

$\therefore$  Design is safe.

3. Helical Gear :-

$$P = 140 \text{ kW}, N_1 = 1440 \text{ rpm}, N_2 = 360 \text{ rpm}, \phi = 20^\circ \text{ FD}, \beta = 25^\circ$$

$$a = 400 \text{ mm.}$$

Sol :-

1. Material Selection :-

↳ Gears - Cast Steel

2. No. of Teeth :- ( $Z_1$  &  $Z_2$ )

$$\begin{aligned} \text{↳ } Z_1 &= 18, Z_2 = i \times Z_1 \\ &\Rightarrow 65 \text{ teeth} \end{aligned}$$

3. Module :-

$$\text{↳ } a = \left( \frac{m_n}{\cos \beta} \right) \left( \frac{Z_1 + Z_2}{2} \right)$$

$$m_n \Rightarrow 7.25 \approx 8 \text{ mm}$$

4.  $d$ ,  $v$  &  $b$  :-

$$\text{↳ } d_1 = \frac{10 m_n}{\cos \beta} \times Z_1$$

$$\Rightarrow 176 \text{ mm}$$

$$\text{↳ } b \Rightarrow 10 m_n \Rightarrow 80 \text{ mm}$$

$$\text{↳ } v \Rightarrow \frac{\pi d_1 N_1}{60 \times 1000} \Rightarrow 13.0 \text{ m/s.}$$

5. Beam Strength :- ( $F_s$ )

$$F_s \Rightarrow \pi \times m_n \times b \times [\sigma_b] \times y_v$$

$$\boxed{F_s \Rightarrow 27.0 \times 10^3 \text{ N}}$$

6.  $F_d$  :-

$$F_d = F_T + \left[ \frac{0.164 V_m (C_b \cos^2 \beta + F_T) \cos \beta}{0.164 V_m + 1.485 \sqrt{C_b \cos^2 \beta + F_T}} \right]$$

$$\boxed{F_d = 46.86 \text{ kW}}$$

7.  $F_w$  :-

$$F_w = \frac{d_1 \times b \times \rho \times k}{\cos^2 \beta}$$

$$\boxed{F_w \Rightarrow 88.8 \text{ kW}}$$

8. checking ( $F_w$ )

$$F_w > F_d \text{ (Safe)}$$

9. checking ( $F_s$ )

$$F_s > F_d \text{ (Safe)}$$

1. Design a cast iron bevel gear drives for a pillar drilling m/c to transmit 1875 W at 800 rpm. to a spindle at 400 rpm. The gear is to work for 40 hours per week for 3 years. Pressure angle is  $20^\circ$ .

Given :-

$$\rightarrow P = 1875 \text{ W}$$

$$\rightarrow N_1 = 800 \text{ rpm}$$

$$\rightarrow N_2 = 400 \text{ rpm}$$

$$\rightarrow i = 2$$

$$\rightarrow T = 40 \times 52 \times 3 = 6240 \text{ cycles}$$

$$\alpha = 20^\circ$$

1. Material :-

$$\rightarrow \text{Gears} - \text{C45} \quad [8.5]$$

2.  $[\sigma_c]$  and  $[\sigma_b]$

$$\rightarrow [\sigma_c] = C_B \text{ HB } K_{ca} \text{ (or) } C_R \text{ HRC } K_{ca} \quad [8.18]$$

$$C_B = 23$$

$$\text{HB} = 260$$

$$K_{ca} = 0.636$$

$$K_{ca} = 6 \sqrt{\frac{10^7}{N}}$$

$$\therefore N = 60NT$$

$$\Rightarrow 60 \times 400$$

$$\times 6240$$

$$\Rightarrow 149.7 \times 10^6$$

$$[\sigma_c] = 23 \times 260 \times 0.636$$

$$[\sigma_c] \Rightarrow 380.328 \text{ N/mm}^2$$

$$\hookrightarrow [\sigma_b] = \frac{1.4 K_{bl} \sigma_{-1}}{n K_{\sigma}}$$

$$\rightarrow K_{bl} \Rightarrow 0.685$$

$$\sigma_{-1} \Rightarrow 0.4 \sigma_u \quad \because \sigma_u = 350 \text{ N/mm}^2$$

$$\rightarrow \sigma_{-1} = 157.5 \text{ N/mm}^2$$

$$\rightarrow n = 2.0$$

$$\rightarrow K_{\sigma} = 1.2$$

$$\therefore [\sigma_b] = 62.93 \text{ N/mm}^2$$

3. Gear ratio and pitch angle :- ( $\delta_1$  &  $\delta_2$ )

$$\hookrightarrow i = 2$$

$$\hookrightarrow \tan \delta_2 = i$$

$$\delta_2 = 63.43^\circ$$

$$\delta_1 = 90 - 63.43 \Rightarrow 26.57^\circ$$

4. Cone distance :-

$$R \geq \psi_y \sqrt{i^2 + 1} \sqrt[3]{\left(\frac{0.72}{\psi_y - 0.5(\sigma_u)}\right)^2 \frac{E(M_T)}{i}} \quad (8.13)$$

$$R = 71.63 \text{ mm (or) } 72 \text{ mm}$$

5. No. of teeth :- ( $z_1$  &  $z_2$ )

$$z_1 = 18, z_2 = i \times 18 = 36 \text{ teeth.}$$

Transverse module :- ( $M_t$ )

$$M_t = \frac{R}{0.5 \sqrt{z_1^2 + z_2^2}}$$

$$= 3.21 \text{ mm}$$

(8.2)

$$\rightarrow \boxed{M_t = 3.5 \text{ mm}}$$

7. Cone distance :-

$$D = 0.5 M_t \sqrt{z_1^2 + z_2^2} \quad (8.28)$$

$$\boxed{R = 79 \text{ mm}}$$

8. cal.  $b, v, d$  :-

$$\rightarrow d_{av_1} = m_{av} \times z_1, \quad d_{av_2} = m_{av} \times z_2$$

$$m_{av} = M_t - \frac{b \sin \delta_2}{20}$$

$$m_a = 2.91 \text{ mm}$$

$$\therefore d_{av_1} = \underline{58.22 \text{ mm}} //$$

$$\rightarrow v = \frac{\pi d_{av_1} N_1}{60 \times 1000} \Rightarrow \underline{2.43 \text{ m/s.}} //$$

$$\rightarrow b = R / \psi_y = \underline{26.33 \text{ mm}} //$$



9. Torque :-  $(M_T)$

$$(M_T) = M_T \cdot k \cdot kd$$

$$= 22.38 \times 10^3 \times 1.1 \times 1.35$$

$$(M_T) \Rightarrow 33.23 \times 10^3 \text{ N-mm}$$

10. checking  $(\sigma_b)$  and  $(\sigma_c)$

$$(\sigma_b) = \frac{R \sqrt{l^2 + 1} (M_T)}{(R - 0.5b)^2 b m y_v} \cdot \frac{1}{\cos \alpha} \leq [\sigma_b]$$

$$(\sigma_b) \Rightarrow 37.78 \text{ N/mm}^2$$

$$(\sigma_c) = \frac{0.72}{(R - 0.5b)} \cdot \frac{\sqrt{(\sqrt{l^2 + 1})^3}}{i \times b} \times \Sigma(M_T) \leq [\sigma_c]$$

$$(\sigma_c) \Rightarrow 351.01 \text{ N/mm}^2 \leq [\sigma_c]$$

11. Parameter :-

$$\rightarrow m_f = 3.5 \text{ mm}$$

$$\rightarrow z_1 = 18, z_2 = 36 \text{ teeth}$$

$$\rightarrow R = 79 \text{ mm}$$

2. Bevel Gear drives to transmit 3.5 kW. at Speed ratio of 4. Driving shaft = 200 rpm. Non-reversible pinion is of Steel and wheel of CI. Assume gear life = 25,000 hrs.

Given data :-

↳  $P = 3.5 \text{ kW}$ ,  $i = 4$ ,  $N_2 = 200 \text{ rpm}$ ,  $T = 25,000 \text{ hrs}$ .

1. Materials :-

↳  $\begin{cases} \text{Gears} - \text{CI} \\ \text{pinion} - \text{Steel} \end{cases}$

2. 'i' and  $(\delta_1 \& \delta_2)$

↳  $i = 4$ ,

↳  $\tan \delta_2 = i$

$$\delta_2 = 75.96^\circ$$

$$\delta_1 = 90 - 75.96$$

$$\Rightarrow 14.04^\circ$$

3.  $[\sigma_b]$  and  $[\sigma_c]$

$$[\sigma_c] = C_R HRC K_{cf}, C_{BHB} K_{cf}$$

$$[\sigma_c = 339.06 \text{ N/mm}^2]$$

$$C_R \geq 23$$

$$HRC \geq 260$$

$$K_{cf} = 0.567$$

$$[\sigma_B] \Rightarrow \frac{1.4 k_{bl} \sigma_{-1}}{n k_{\sigma}}$$

$$\Rightarrow \frac{1.4 \times 1 \times 220}{2 \times 1.2}$$

$$\Rightarrow 91.66 \text{ N/mm}^2$$

$$k_{bl} = 1$$

$$\sigma_{-1} = 220 \quad (8.5)$$

$$n = 2.0$$

$$k_{\sigma} = 1.2$$

4. Cone distance  $:(R_{\min})$

$$R_{\min} \geq \psi_y \sqrt{(i^2 + 1)} \sqrt[3]{\left( \frac{0.72}{(\psi_y - 0.5) (\sigma_H)} \right)^2 \frac{E(M_T)}{b}}$$

$$\geq 139.35 \text{ mm} \approx 140 \text{ mm}$$

$$\psi_y = 3$$

$$(M_T) = M_T \times \frac{K \times K_d}{1.3}$$

$$\downarrow$$

$$M_T = \frac{P \times 60}{2 \pi n}$$

5.  $m_t$  :- (module)

$$m_t = \frac{R}{0.5 \sqrt{z_1^2 + z_2^2}}$$

$$\Rightarrow \frac{140}{0.5 \sqrt{18^2 + 30^2}}$$

$$\boxed{m_t \Rightarrow 4 \text{ mm}}$$

6.  $R$  :-

$$R = 0.5 m_t \sqrt{z_1^2 + z_2^2}$$

$$\boxed{R = 182 \text{ mm}}$$

7.  $m_{av}$ ,  $d_{av}$ , &  $v$  :-

$$\hookrightarrow m_{av} = m_t - \frac{b \sin \delta_1}{z_1}$$

$$m_{av} \Rightarrow 3.33 \text{ mm} //$$

$$\hookrightarrow d_{av} = m_{av} \times z_1$$

$$\boxed{d_{av} = 73.26 \text{ mm}} //$$

$$\hookrightarrow v = \pi d_{av} \times N / 60 \times 1000$$

$$\boxed{v \Rightarrow 3.06 \text{ m/s}} //$$

8.  $(M_T)$  :-

$$(M_T) = m_t \cdot k \cdot k_d$$

$$(M_T) \Rightarrow 62.028 \times 10^3 \text{ N-mm} //$$

9. checking  $(\sigma_b)$  &  $(\sigma_c)$  :-

$$(\sigma_c) = \frac{0.72}{(R - 0.5b)} \cdot \frac{\sqrt{(k^2 + 1)^3}}{bb} \times E(M_T)$$

$$(\sigma_c) = 242.75 \text{ N/mm}^2 \leq 339.06$$

$$\therefore (\sigma_c) \leq [\sigma_c] \text{ safe} //$$

$$\# (\sigma_b) = \frac{R \sqrt{k^2 + 1} (M_T)}{(R - 0.5b)^2 b m_{av} Y_v} \times \frac{1}{\cos \alpha}$$

$$= 22.07 \leq 91.66 \text{ N/mm}^2$$

$$\therefore (\sigma_b) \leq [\sigma_b] \text{ safe} .$$

Parameter :-

$$\rightarrow m_t = 4 \text{ mm}$$

$$\rightarrow z_1 = 18, z_2 = 72 \text{ mm}$$

$$\rightarrow R = 180 \text{ mm}$$

$$\rightarrow d_1 = 95.76 \text{ mm}, d_2 = 352.94 \text{ mm}.$$

3. Design a pair of bevel gear to transmit 10kW at 1440 rpm  
Reqd. transmission ratio is 4. material for gears are  
15Ni2Cr1Mo / steel.

Given :-  $P = 10 \text{ kW}, N_1 = 1440 \text{ rpm}, i = 4, \alpha = 20^\circ$

1. material :-

$$\rightarrow \text{Pinion and gears } \frac{15}{\text{Ni 2Cr 1Mo 15}} / \text{steel}.$$

2. Gear ratio and pitch angle :-

$$\rightarrow i = 4,$$

$$\rightarrow \tan \delta_2 = i, \delta_2 = 75.96^\circ$$

$$\delta_1 = 90 - 75.96 \Rightarrow 14.03^\circ$$

3. Teeth :- ( $z_1$  and  $z_2$ )

$$z_1 = 18, z_2 = i \times 18 = 72 \text{ teeth}.$$

4. Tangential load :- ( $F_T$ )

$$F_T = \frac{P \times K_o}{v}$$
$$= \frac{10 \times 10^3 \times 1.25}{1.507 m/s}$$

$$K_o = 1.25$$

$$v = \frac{\pi \times m \times z_1 \times N_1}{60 \times 1000}$$

$$= \frac{\pi \times 4 \times 18 \times 1440}{60 \times 1000}$$

$$F_T \Rightarrow \frac{8294.625}{m_t}$$

5. Dynamic Load :- ( $F_d$ )

$$F_d = C_v \times N_{sf} \times k_m \times F_T$$

$$\therefore F_d \Rightarrow \frac{10401.4}{m}$$

$$C_v = \left( \frac{5.5 \sqrt{V_m}}{5.5} \right)^{1/2}$$

$$= 1.254.$$

$$k_m = 1, N_{sf} = 1.$$

6. Beam Strength ( $F_s$ ) :-

$$F_s = \pi \times m_t \times b \times (\sigma_b) \times y \times \left( \frac{R-b}{R} \right)$$

$$(F_s) \Rightarrow 120 m_t^2$$

$$(\sigma_b) = 320 \text{ N/mm}^2$$

$$y = 0.154 - \frac{0.912}{z_1} = 0.110$$

$$R = 41.23 m_t$$

7. module :- ( $m_t$ )

$$F_s = F_d$$

$$\therefore m_t = 2.31 \text{ mm}$$

$$\text{std } m_t = 3 \text{ mm}$$

8. b, d and  $\varphi$  :-

$$\rightarrow b = 10 \times 3 = 30 \text{ mm} //$$

$$\rightarrow d = m z_1 = 3 \times 18 \Rightarrow 44 \text{ mm} //$$

$$\rightarrow \varphi = \frac{\pi \times d \times N_1}{60 \times 1000} \Rightarrow 4.52 \text{ m/s} //$$

9. Re-cut beam strength  $[F_s] :-$

$$F_s = \pi \times m \times b \times [\sigma_b] \times y \times \left(\frac{R-b}{R}\right)$$

$$\boxed{F_s \Rightarrow 7544.68 \text{ N}}$$

10. Accurate dynamic loading  $:- (F_d)$

$$F_d = F_T + \left[ \frac{0.164V + C_b + F_T}{0.164V + 1.485 \sqrt{C_b + F_T}} \right]$$

$$\boxed{F_d = 2818.55 \text{ N}}$$

11. Max. Wear Load  $:-$

$$F_w = \frac{0.75 \times d_1 \times b \times Q \times k}{\cos \delta_1}$$

$$\boxed{F_w = 2746.84 \text{ N}}$$

12. checking  $F_s$  &  $F_w$   $:-$

$F_s > F_d$   $:-$  Design is safe.

$F_w > F_d$   $:-$  "

13. Parameter  $:-$

$\rightarrow M_c = 3 \text{ mm}$

$\rightarrow \alpha_1 = 18, \alpha_2 = 72 \text{ teeth}$

power gear drives to transmit 7.36 kW at 1440 rpm. Gear ratio 3, material for pinion and gears are C45 hardened

Given :-

↳  $P = 7.36 \text{ kW}$ ,  $N_1 = 1440 \text{ rpm}$ ,  $i = 3$ , C45 steels.

1. Materials :-

↳ Pinion/Gears — C45 steel hardened.

2. No. of teeth :-  $Z_1$  and  $Z_2$

$$Z_1 = 18, Z_2 = 54 \text{ teeth}$$

3. Tangential Load :- ( $F_T$ )

$$F_T = \frac{P \times K_o}{v} \quad \left| \quad v = \frac{\pi D \times N_1}{60 \times 1000} \quad \because D = m Z_1.$$

$$\rightarrow F_T = 6133.3 / m_t$$

4. Dynamic Load :- ( $F_{DL}$ )

$$\rightarrow F_{DL} \Rightarrow F_T \times C_v \times N_{stb} \times K_m \quad \left| \quad C_v = \left( \frac{5.5 + \sqrt{v_m}}{5.5} \right)^{1/2}$$
$$\Rightarrow 6378.66 / m_t$$

5. Beam Strength :- ( $F_s$ )

$$\rightarrow F_s = \pi \times b \times m_t \times [\sigma_b] \times y_v$$

$$F_s = \pi \times 10 m_t \times m_t \times (\sigma_b) \times y_v$$

$$\boxed{F_s = 406.14 m_t^2}$$



6. Modute :- ( $m_t$ )

$$F_s = F_d$$

$$406.14 m_t^2 = \frac{6378.66}{m_t}$$

$$\boxed{m_t = 2.5 \text{ mm}}$$

7. cat,  $B$ ,  $b$ ,  $v$ , and  $d_1$  :-

$$\rightarrow B = 10 \times 2.5 = 25 \text{ mm}$$

$$\rightarrow d_1 = m_t z_1 = 2.5 \times 18 = 45 \text{ mm}$$

$$\rightarrow v = \pi d_1 N_1 / 60 \times 1000 \Rightarrow 3.27 \text{ m/s.}$$

8. Recal beam strength ( $F_s$ ) :-

$$F_s = 406.10 m_t^2$$

$$\boxed{F_s = 2538.375 \text{ N}}$$

9. Dynamic Load :- ( $F_d$ )

$$F_d = F_T + \frac{0.164 V_m (C_b + F_T)}{0.164 V_m + 1.465 \sqrt{C_b + F_T}}$$

$$\boxed{F_d = 8606.77 \text{ N}}$$

10. Max. Wear Load :- ( $F_w$ )

$$F_w = d_p \cdot Q \cdot k \cdot b \times \frac{1}{\cos \alpha}$$

$$\boxed{F_w = 2754.7 \text{ N}}$$